

$$\varrho = \frac{r}{r_{(1)}}, \quad \varrho_1 = \frac{r_v}{r_{(1)}}. \quad (1)$$

After this arrangement any spiral path is defined by one basic parameter only

$$E_{(1)} = 1 / \left(\frac{v}{v_{esc}} \right)_{(1)}^2 = \frac{2GM}{r_{(1)}v_{(1)}^2}, \quad (2)$$

provided the magnetic field is dipolar. $E_{(1)}$ defines the rate v/v_{esc} at the level $r_{(1)}$.

Since, however, the magnetic field is often far from being dipole, the variation of the magnetic field will rather be expressed by

$$H/H_{(1)} = \varrho^{-n} \quad (n > 1) \quad (3)$$

in the considered region, and n is now another basic parameter (n need not equal 3).

If (e. g., after a collision) only the velocity (E) and the direction (i) known at a given level r (in km), $E_{(1)}$ is obtained from

$$E_{(1)} = \frac{E\varrho}{E\varrho - (E - 1)}, \quad (4)$$

where ϱ is gained by solving

$$\varrho^n \sin^2 i - E\varrho + E - 1 = 0 \quad (5)$$

and $r_{(1)}$ is found from (5) and (1).

The path formula (variation of i with ϱ) is

$$\sin i = 1 / [E_{(1)}\varrho^{n-1} - (E_{(1)} - 1)\varrho^n]^{1/2} = \frac{v_{\perp}}{v}. \quad (6)$$

Some other path parameters like the velocity v , its component perpendicular to H , v_{\perp} , the path radius R , the other level of reflection $r_{(2)}$, the critical level r_w with $i = \text{minimum}$ are

$$R/R_{(1)} = \varrho^{n/2} \quad (7)$$

$$v_{\perp}/v_{\perp(1)} = \varrho^{-n/2} \quad (8)$$

$$v/v_{(1)} = \sqrt{[E_{(1)}/\varrho - (E_{(1)} - 1)]} \quad (9)$$

$$\Sigma_{(1)} = \sum_{j=0}^n \varrho_{(2)}^{-j} \quad \left(\varrho_{(2)} = \frac{1}{E_{(1)} - 1} \right) \text{ for } n=2 \quad (10)$$

$$\varrho_{(2)} = \frac{r_{(2)}}{r_{(1)}} = \frac{0.5 + \sqrt{(E_{(1)} - 3/4)}}{E_{(1)} - 1} \quad (10\text{-dipole})$$

$$S_w = \frac{E_{(1)}}{n} \cdot \frac{n-1}{E_{(1)}-1}; \quad v_w = v_{esc}/\sqrt{n}; \quad E_w = n;$$

$$\sin i_w = \left(\frac{E_{(1)}-1}{n-1} \right)^{(n-1)/2} \left(\frac{n}{E_{(1)}} \right)^{n/2}. \quad (11)$$

The level at which i has a given value is found by solving

$$\varrho^n - \frac{E_{(1)}}{E_{(1)}-1} \varrho^{n-1} + \frac{1}{(E_{(1)}-1) \sin^2 i} = 0. \quad (12)$$

If collisions are taken into account (keeping in mind that before and after a collision the same number of particles gains the direction $i > 60^\circ$ as $i < 60^\circ$), the deductions A, B, C, can be drawn. They are briefly explained as follows: In higher, less dense regions the particle rather slides than circles (i is smaller); thus after a collision it is probable that i increase more than in deeper, more dense parts (near the magnetic mirror where i approaches 90°). After an increase of i (i. e. when the path becomes more perpendicular the spirals more squeezey) also the mean magnetic mirror shifts upwards, impeding the particles of the plasma jet in reaching the stellar surface again. Thus, the collisions near the mean magnetic mirror rather cause a downshift of the exploded gas, and the collisions which occur in the upper parts of the plasma jet contribute to its turning into apparently motionless, stable arcs, or clouds, even though their inner motion is $v \geq v_{esc}$.

(A) Conditions favourable for trapping an exploded gas are:

(A1) Velocity at the magnetic mirror high above $v_w \approx 1/2 v_{esc}$

(A2) Collisions far from r_H and r_g : Between the two levels with $i = 60^\circ$.

(A3) The mean velocity must not decrease for other reasons than gravity.

(A4) The top of the field line must be high above the lower level with $i = 60^\circ$.

(A5) The magnetic field varies so that n increases.

(B) An expansion and falling of the exploded stream is expected when opposite phenomena occur (B1) — (B5).

(B6) In polar regions, where the top of the field line is practically infinite, trapping is excluded on account of the rapid spread of the plasma jet towards the interstellar space.

(C) With respect to (A4) and (B6), a plasma exploded from the whole stellar surface becomes trapped and condensed only when it streams from relatively high latitudes but far from the poles. Thus usually a thin, hollow torroid is created, which hovers apparently motionless above the stellar equator.

Also phenomena observed above the photosphere are usually governed by the above theorem. (Below the photosphere a rather chaotic motion prevails, $p_{\text{kin}} > p_{\text{magn}}$). If we consider the big magnetic tubes situated below the photosphere, which increase in intensity during the solar cycle, we reach the following conclusions; when $p_{\text{grav}} < p_{\text{kin}} + p_{\text{magn}}$ the region should explode. The surrounding space impedes an immediate explosion. When, however, the magnetic tube rises and expands slightly, it is far from the dipolar case. A very slight decrease of the intensity H (about 1%) which occurs between the levels r_0 and $1.001 r_0$ represents an extremely high value of $n \approx 10$. As to (A5), the trapping and squeezing towards the top of the magnetic field line is very strong.

Prominences: When particle velocities inside an explode plasma jet exceed the velocity $v_w \approx \frac{1}{2} v_{\text{esc}}$, the stream becomes trapped and turns into an apparently motionless stable prominence or filament. When the squeezing towards the top is too high, so high that $p_{\text{kin}} > p_{\text{magn}}$, the whole configuration collapses, some parts are ejected, afterwards they fall down freely, to levels of sufficiently high H .

Flares: An increase of the subphotospheric magnetic field with a very high n brings about strong squeezing towards the magnetic zero-line, which represents the top of the magnetic loops.

A brilliant point arises in the middle between two sunspots of different polarity.

Proton flares: If many big magnetic "tubes" are compressed above the surface, the uppermost parts can dissolve into the outer parts of the chromosphere in the form of prominences, while in the most inner region the trapping is weak (the top is too low, the time m sufficient for real trapping and squeezing towards the top). Thus, again, a large tunnel, or a large bubble, arises, in which the inner plasma is compressed severely towards the magnetic zero-line where a filamentary flare develops. After a relatively short time either the magnetic field lines deform so that n shifts from about 10 towards 3, or the particle velocity decreases (due to losses by energy exchange). Both effects result in a downward shift of the mean magnetic mirror. The maximum plasma density shifts downwards along the field lines and, since one sees more particles tangentially to the field line, than when looking across, the central filament splits into two filaments, slightly deviating from each other. They can be observed well just above the chain of sunspots, because we are now looking tangentially to the shell.

Some details showing, e. g., how the character of the stream changes, if the velocity, the magnetic field variation (n -) and the direction gradually change at the points of collision, are given in several tables by Woyk (1972b) and the derivation of the mentioned formulae is indicated by Woyk (1972a).

References

WOYK, E. (1972a): Bull. Astron. Inst. Czech., 23, 272.

WOYK, E. (1972b): Bull. Astron. Inst. Czech., 23, 279.